

$$(1) \quad G(s) = \frac{6(s+5)}{s(s+1)(s+3)(s+10)}$$

This is a type 1 system

Therefore, steady state error is zero for the step input.

Now, for ramp input,

$$e_{ss} = \frac{A}{K_v}$$

$$K_v = \lim_{s \rightarrow 0} s \cdot G(s)$$

$$= \lim_{s \rightarrow 0} s \cdot \frac{6(s+5)}{s(s+1)(s+3)(s+10)}$$

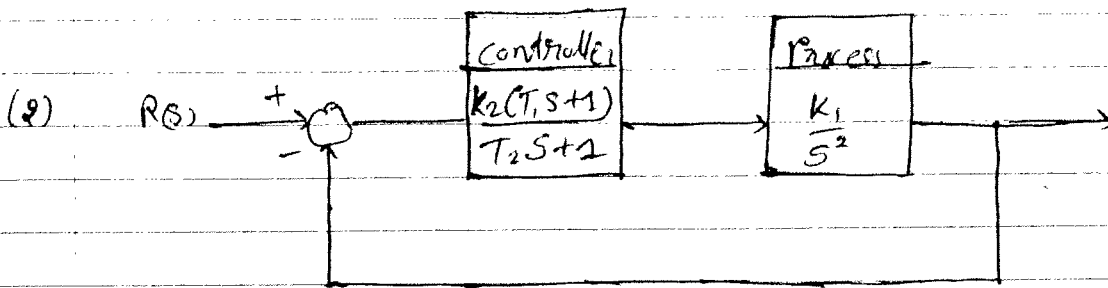
$$= \frac{5 \times 6}{1 \times 3 \times 10}$$

$$K_v = 1$$

$$\therefore \text{steady state error } e_{ss} = \frac{A}{K_v}$$

$$= \frac{A_0}{1}$$

$$\boxed{e_{ss} = A_0}$$



$$T_1 = 1$$

$$T_2 = 0$$

$$\therefore K(s)G(s) = \frac{k_1 k_2 (s+1)}{s^2}$$

$$\therefore \text{Transfer function} = \frac{k_1 k_2 (s+1) / s^2}{1 + k_1 k_2 (s+1) / s^2}$$

$$= \frac{k_1 k_2 (s+1)}{s^2 + k_1 k_2 s + k_1 k_2}$$

assume  $\xi = 0.70$

$$\omega_n = \sqrt{k_1 k_2}$$

$$\therefore 2\xi\omega_n = k_1 k_2$$

$$2\xi\sqrt{k_1 k_2} = k_1 k_2$$

$$\therefore 4\xi^2 = k_1 k_2$$

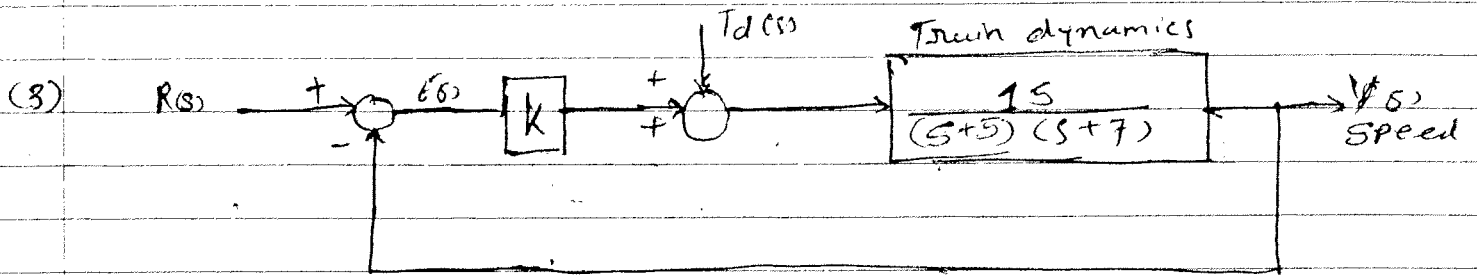
$$k_1 k_2 = 1.96$$

now, checking the value for  $k_1$  &  $k_2$

$$T_s = \frac{4}{\xi\omega_n} = \frac{4}{0.98} \approx 4 \text{ sec} \quad \text{this is very slow response}$$

now @ at  $\xi = 1 \Rightarrow T_s = \frac{4}{\xi\omega_n} = \frac{4}{2} = 2 \text{ sec}$

Therefore, value for the  $k_1 k_2$  should be greater than 1.96



(a) 
$$e_{ss} = \frac{1}{1+K_p} \quad \& \quad Y(s) = \frac{15K}{(s+7)(s+5)+15K} R(s) + \frac{15}{(s+7)(s+5)+15K} T_d(s)$$

$$K_p = \lim_{s \rightarrow 0} \frac{15K}{(s+5)(s+7)}$$

$$= \frac{15K}{35}$$

now,

$$K=1, \quad K_p = 0.3, \quad e_{ss} = 0.76$$

$$K=10, \quad K_p = 4.28, \quad e_{ss} = 0.186$$

$$K=100, \quad K_p = 42.85, \quad e_{ss} = 0.0228$$

(c) 
$$\frac{Y(s)}{T_d(s)} = \frac{15}{(s+7)(s+5)+15K}$$

$$= \frac{15}{s^2 + 12s + 35 + 15K}$$

$$\left[ \frac{Y(s)}{T_d(s)} \right]_{max} = \frac{15}{35 + 15K}$$

now

$$K=1 \Rightarrow (Y/T_d)_{max} = 0.3$$

$$K=10 \Rightarrow (Y/T_d)_{max} = 0.081$$

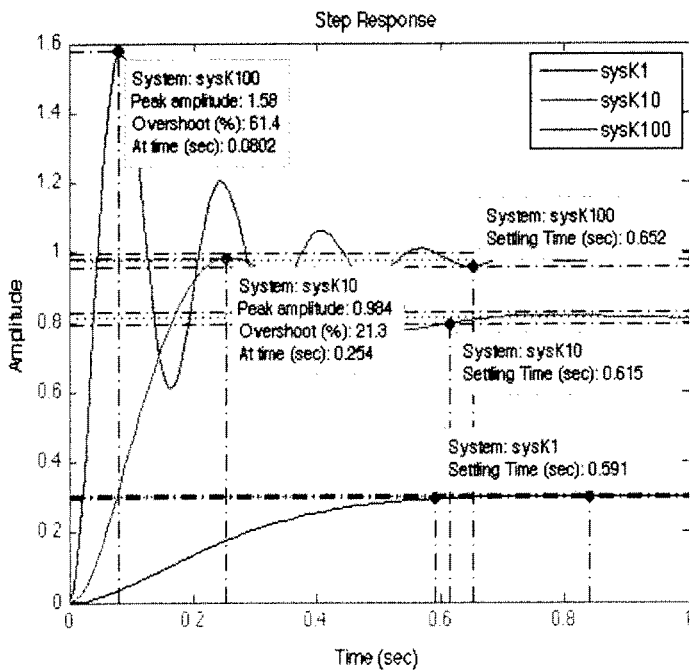
$$K=100 \Rightarrow (Y/T_d)_{max} = 0.0097$$

K	$e_{ss}$	$(Y/T_d)_{max}$	$T_s$	P.O.
1	0.76	0.3	0.594	0
10	0.186	0.081	0.615	21.3
100	0.0228	0.0097	0.652	61.4

$\Rightarrow$  best compromise value for

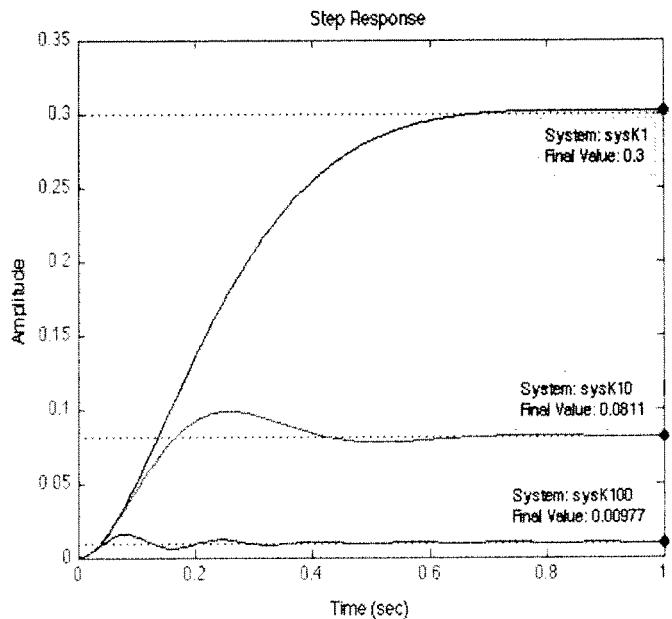
Step response for Y(s), R(s)

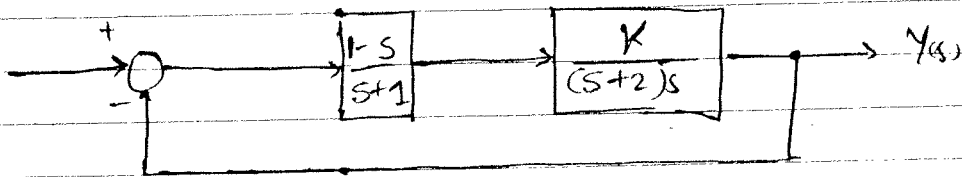
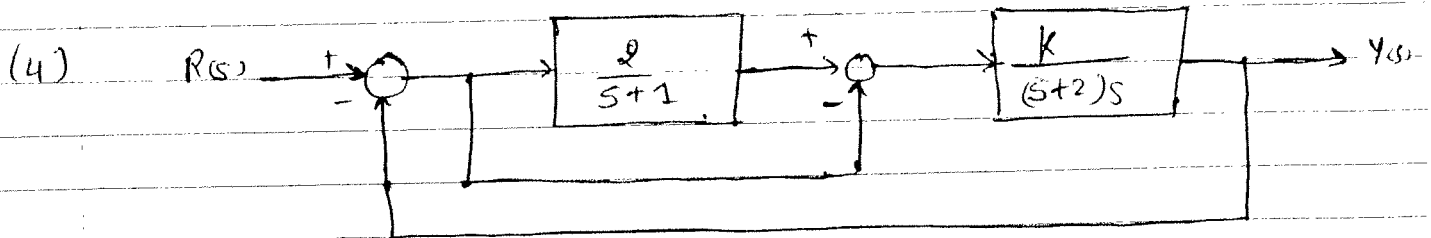
```
>> num=15;
>> den=[1 12 50];
>> sysK1=tf(num,den)
Transfer function:
      15
-----
s^2 + 12 s + 50
>> step(sysK1)
>> hold on
>> num=150;
>> den=[1 12 185];
>> sysK10=tf(num,den)
Transfer function:
      150
-----
s^2 + 12 s + 185
>> step(sysK10)
>> hold on
>> num=1500;
>> den=[1 12 1535];
>> sysK100=tf(num,den)
Transfer function:
      1500
-----
s^2 + 12 s + 1535
>> step(sysK100)
```



Step response for Td(s), Y(s)

```
>> num=15;
>> den=[1 12 50];
>> sysK1=tf(num,den)
Transfer function:
      15
-----
s^2 + 12 s + 50
>> step(sysK1)
>> hold on
>> den=[1 12 185];
>> sysK10=tf(num,den)
Transfer function:
      15
-----
s^2 + 12 s + 185
>> step(sysK10)
>> hold on
>> den=[1 12 1535];
>> sysK100=tf(num,den)
Transfer function:
      15
-----
s^2 + 12 s + 1535
>> step(sysK100)
```





$\therefore$  characteristic eq<sup>n</sup> =  $1 + G(s)K(s) = 0$

$$\therefore 1 + \frac{K}{(s+2)s} \times \frac{(1-s)}{(s+1)} = 0$$

$$\therefore s(s+2)(s+1) + K - Ks = 0$$

$$\therefore s^2 + 3s^2 + 2s + Ks + K = 0$$

$$s^2 + 3s^2 + (2-K)s + K = 0$$

$s^3$	1	$(2-K)$
$s^2$	3	K
$s^1$	$\frac{3(2-K)-K}{3}$	0
$s^0$	K	

$$K=0 \quad \& \quad \therefore \frac{3(2-K)-K}{3} = 0$$

$$\therefore 6 - 4K = 0$$

$$K = \frac{6}{4}$$

$$K = 1.5$$

therefore, range of K is  $0 < K < 1.5$  for stable system. otherwise ~~system~~ any value of K system goes unstable

$$(5) \quad L(s) = \frac{k(s+2)}{s(s-1)}$$

$$= \text{Characteristic eqn} = 1 + \frac{k(s+2)}{s(s-1)} = 0$$

$$\therefore s(s-1) + k(s+2) = 0$$

$$\therefore s^2 - s + ks + 2k = 0$$

$$s^2 + (k-1)s + 2k = 0$$

$$\omega_n = \sqrt{2k}$$

$$2\zeta\omega_n = k-1$$

$$\text{Now } \zeta = 0.707$$

$$2(0.707)\sqrt{2k} = k-1$$

$$\therefore 2(0.499)2k = k^2 - 2k + 1$$

$$\therefore 4k = k^2 - 2k + 1$$

$$k^2 - 6k + 1 = 0$$

$$= \frac{+6 \pm \sqrt{36-4}}{2}$$

$$= \frac{+6 \pm \sqrt{32}}{2}$$

$$\therefore k = 5.825 \quad \& \quad k = 0.175$$

For stability  $k$  must be greater than 1.

$$\boxed{\therefore k = 5.825}$$