

# MCE441: Intr. Linear Control Systems

Lecture 2: Control Engineering Cycle  
Open-Loop and Closed-Loop  
Positive vs Negative Feedback  
Mathematical Models  
Dynamic Modeling of Engineering Systems

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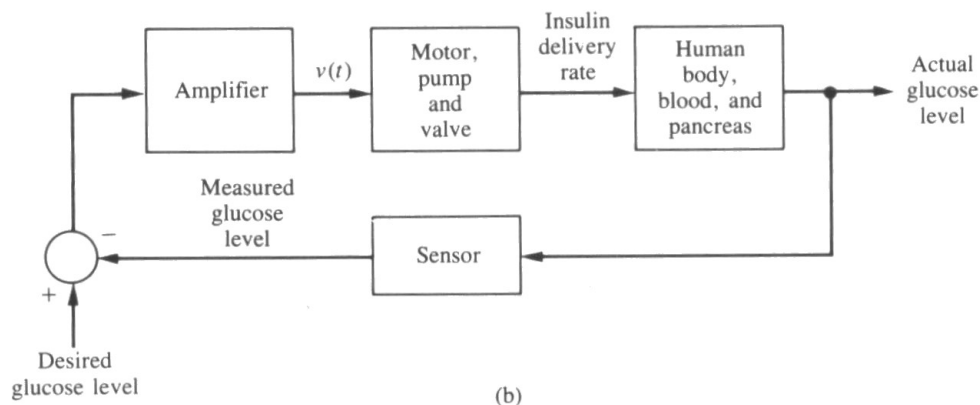
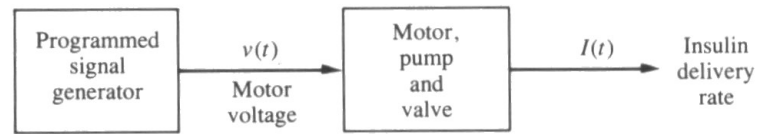
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## Open Loop and Closed Loop Control

- Open Loop (feedforward): Control input independent of output: Scheduling
- Useful with no uncertainties, no unpredictable disturbances: Know the future
- Closed Loop (feedback): Control input depends on output: Fundamental error correction mechanism
- If *judiciously* used, can reject disturbances, maintain stability and performance in the face of uncertainties.
- It can destabilize an open-loop stable system. Details later.

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# Feedforward vs Feedback: Example



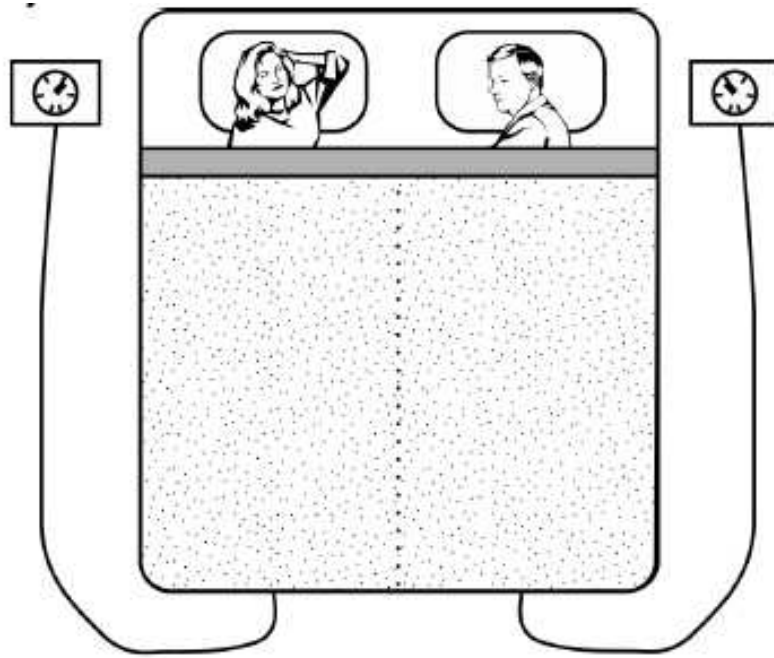
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## Negative vs. Positive Feedback

- **Negative Feedback:** The fed back output and the reference input are subtracted
- Negative feedback has an error-compensating effect
- Still, too much or too little feedback can be destabilizing
- **Positive Feedback:** The fed back output and the input are added
- Positive feedback has a destabilizing effect
- Still, some systems can tolerate some positive feedback and remain stable. *More later...*

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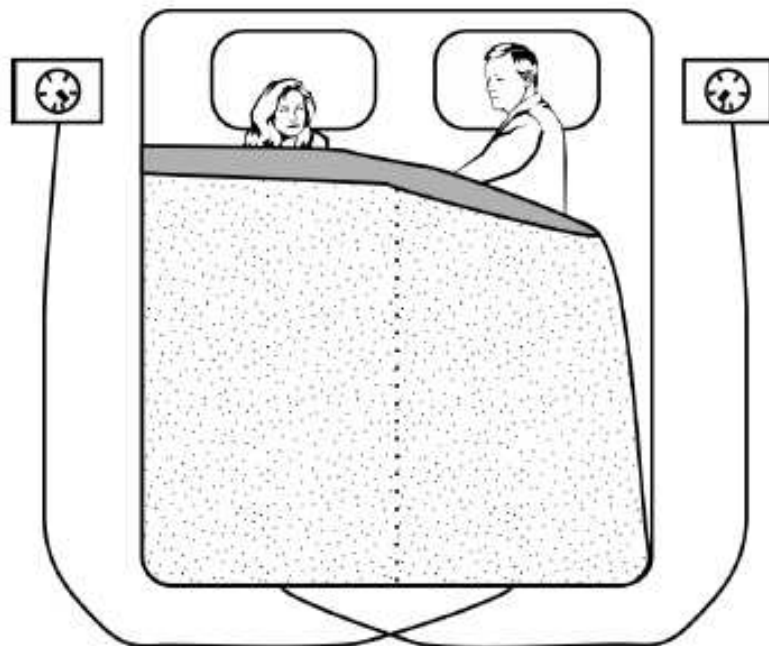
# Negative Feedback - Usually good



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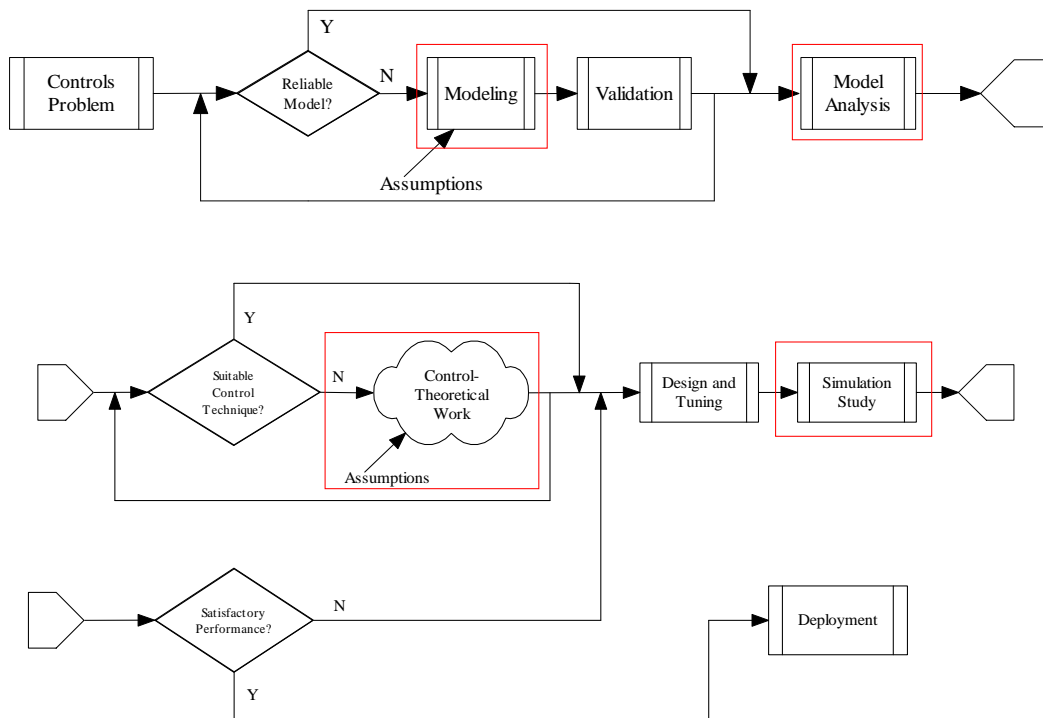
# Positive Feedback - Usually bad



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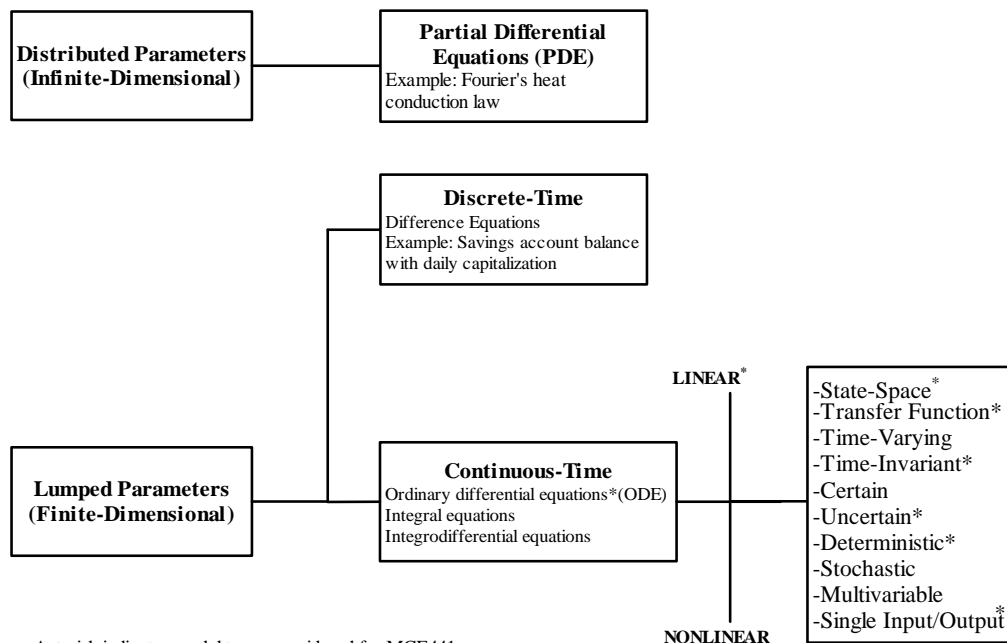
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# Control Design Cycle



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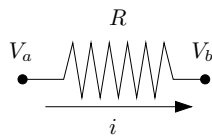
# Classification of Models



Asterisk indicates model types considered for MCE441  
Linear, time-invariant, single input, single output systems are denoted as SISO-LTI

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# Dynamic Modeling of Electrical Systems

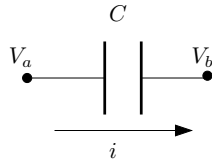


## Linear Resistor

Variables:  
Current  $i$ : Amperes (A)  
Voltage  $V_{ab}$ : Volts (V)  
Parameters:  
Resistance  $R$ : Ohms ( $\Omega$ )  
 $1 \text{ A} = 1 \text{ V/A}$

Law:

$$i = \frac{V_a - V_b}{R}$$



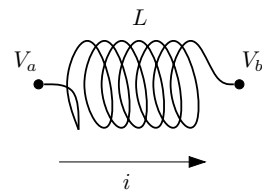
## Ideal Capacitor

Variables:  
Charge  $q$ : Coulomb (C)  
Parameters:  
Capacitance  $C$ : Farad (F)  
 $1 \text{ A} = 1 \text{ F.V/s}$   
 $1 \text{ C} = 1 \text{ F.V}$

Laws:

$$i = C \frac{dV_{ab}}{dt}$$

$$q = CV_{ab} \text{ (integral form)}$$



## Ideal Inductor

Parameters:  
Inductance  $L$ : Henry (H)  
 $1 \text{ V} = 1 \text{ H.A/s}$

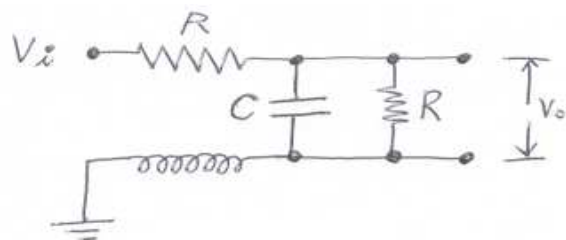
Law:

$$V_{ab} = L \frac{di}{dt}$$

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## electrical systems...

- Other elements: Op-Amps, Diodes (non-linear) presented later, if needed
- Kirchhoff's Laws:
- **Voltage Law**: "The sum of voltage differences around a loop must equal zero"
- **Current Law**: "The sum of currents at a node must be zero"
- Simple example: Find the input/output differential equation (in terms of  $V_o$  and  $V_i$ ):

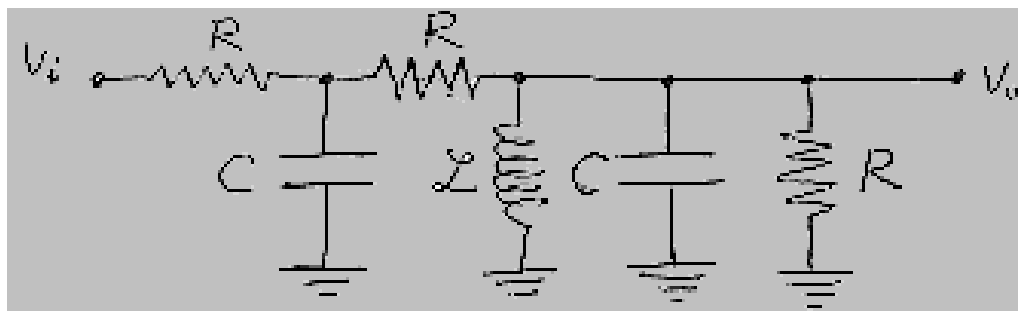


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# Solution

## More difficult example

Find the input/output differential equation (in terms of  $V_o$  and  $V_i$ ):



# Solution

We can easily write all equations describing the system. Elimination of unwanted variables to produce the desired I/O equation can be difficult and tedious. The Laplace transform will greatly facilitate the process.

# Solution

# Solution

Exercise: Check that the required equation is

$$(RC)^2 \ddot{V}_o + 4RC \dot{V}_o + \left(3 + \frac{R^2 C}{L}\right) V_o = V_i$$